Statistics 110 – Assignment 1

Due: Wednesday, July 5, 2006

- 1. Rice 1.17 (Note that this means chapter 1, question 17 from Rice)
- 2. Rice 1.20
- 3. Rice 1.22
- 4. (a) Prove Boole's inequality (for n = 2):

$$P[A \cup B] \le P[A] + P[B]$$

(b) Use induction to generalize Boole's inequality to n events, i.e. show

$$P[A_1 \cup A_2 \cup \ldots \cup A_n] \le P[A_1] + P[A_2] + \ldots + P[A_n]$$

- 5. Rice 1.50, 1.51
- 6. Rice 1.54
- 7. Rice 1.56
- 8. Rice 1.60
- 9. Rice 1.62
- 10. Rice 1.76
- 11. Rice 1.78
- 12. In any given year a male automobile policyholder will make a claim with probability p_m , and a female policyholder will make a claim with probability p_f , where $p_m \neq p_f$. The fraction of policyholders that are male is $\alpha, 0 < \alpha < 1$. A policyholder is chosen at random. If A_i denotes the event that this policyholder makes a claim in year *i*, show that

$$P[A_2|A_1] > P[A_1]$$